## ifo

## Diskussionsbeiträge

No. 88

# Search and the Positive Wage Correlation across Occupations 

Christian Holzner

## Discussion Papers

March 2004

# Search and the Positive Wage Correlation across Occupations 

Christian Holzner ${ }^{\square}$<br>Ifo Institute for Economic Research, Poschingerstr. 5, 81679 Munich, Germany<br>Tel: +49(0)89/9224-1278; Fax: +49(0)89/92241608; E-mail: holzner@ifo.de

## March 2004


#### Abstract

This paper extends the equilibrium search model of Burdett and Mortensen by introducing two different occupations. Local monopsony power and the complementarity of the occupations in production imply that firms occupy the same position in the wage distribution of each occupation. The model also solves for the explicit occupation-specific wage distribution and links them via the production function. Due to search frictions fewer individuals choose the occupation with high education cost compared to the first best. Furthermore, wages of higher educated workers are more compressed than wages of lower educated workers, because firms can extract more search rent from higher educated workers.


Keywords: occupational choice, wage correlation and distribution.

JEL Classification: J21, J31, J41, J42.

[^0]
## 1 Introduction

This paper extends the Burdett-M ortensen (1998) model of equilibrium on-thejob search by introducing two di $\square$ erent occupations. This extension allows for the analysis of firms' wage posting behavior, where firms compete for workers of di■erent occupations. It is shown that firms will post these wages, such that they occupy the same position in the wage o $\square$ er distribution for all occupations. This positive correlation between the wages of workers in di■erent occupations within firms is a well established fact. K atz and Summers (1989) show evidence that secretaries earn more where average wages are higher. M ore recently, B arth and Dale-OIsen (2003) find that "[h]igh-wage establishments for workers with higher education are high-wage establishments for workers with lower education as well." The explanation provided in this paper rests on two things. Firstly, labor market frictions lead to an upward sloping labor supply curve for each occupation. This results from the fact that on-the-job search implies that the higher the wage oПer the more employed workers are attracted from firms o■ering lower wages and the less workers quit to employers paying higher wages. This leads to a higher steady-state occupation size for firms oПering higher wages. Secondly, I need the assumption of complementarity of the occupations in the production process. This guarantees that increasing both labor inputs simultaneously is optimal.

Similar ingredients are also used by K remer (1993) in his O-ring theory to explain the same observation. The production function he proposes exhibits high complementarity of the working colleagues' abilities not to make a mistake, since a mistake results in wasted output regardless of the performance of others. Thus, firms recruit equal ability types for each task (occupation). Since higher ability types are more productive, they are paid higher wages in a competitive market. Thus wage di $\square$ erentials in the 0 -ring theory are attribut-
able to workers' ability, whereas wage di $\square$ erentials in the paper presented here are explained by e! ciency turnover wages.

The O-ring theory also suggests that wages increase with the number of tasks performed in a firm, since only high ability workers are able to produce goods requiring many tasks. Thus, the 0 -ring theory implies a positive correIation between wages and the number of tasks and therefore the overall size of the workforce, whereas this paper predicts a positive correlation between skillgroup size and wages. The findings of Barth and Dale-Olsen (2002) indicate that the employer-size wage e $\square$ ect vanishes once they look at the skill-group size, thus they provide empirical evidence in favour of the labor market frictions approach in this paper compared to the 0-ring theory.

The fact that firms occupy the same position in the wage distribution for each occupation is essential for the derivation of the explicit occupation-specific wage o o er distributions. The occupation-specific wage o oler distributions have the same drawback as in the simple version by Burdett and M ortensen (1998) for a homogenous workforce, namely that the derived increasing left skewed density is at odds with the empirical observation of a log-normal wage earnings density. A ggregation over all occupations, however, yields a spiky, righttailed density if the production elasticities increase for occupations with lower cost of education, an assumption supported by many empirical studies (see Hamermesh 1996, chapter 3). The theory presented in this paper thus puts a systematic structure on the heterogeneity in occupations and industries, which empirical researcher such as K iefer and Neumann (1993), K oning et al. (1995), and van den Berg and Ridder $(1993,1998)$ introduced in an ad hoc way to estimate the simple version of the Burdett-M ortensen model.

This model is not the first one that extends the Burdett-M ortensen model in order to generate a more realistic-shaped wage distribution. M ortensen
(1990) and Burdett and Mortensen (1998) combine their simple model with atomless ex-ante worker heterogeneity, as in the model of Albrecht and A xell (1984). However, this generally does not generate a right-tailed distribution. M ortensen (1990) introduced di $\square$ erences in firm productivity and showed that more productive employers pay higher wages. B ontemps et al. (2000) and Burdett and Mortensen (1998) formulate a closed-form solution for a continuous atomless productivity distribution, which translates into a right-tailed wage earnings distribution, depending on the assumed productivity dispersion. The heterogeneity in productivity across occupations generated in my model is an equilibrium outcome where the occupation-specific marginal products account for the di $\square$ erences in the cost of education and the degree of search frictions in the labor market. The di $\square$ erences in the marginal products are therefore above the first best competitve level.

Hence, the model allows us to analyse the influence of search frictions on the shape of the wage distribution. It is shown that higher search frictions lead to larger wage di $\square$ erentials across occupations for given di■erences in the cost of education. Futhermore, search frictions give each firm some local monopsony power, which each firm uses to extract some rent from its workers. This search rent depends on the degree of labor market frictions and is higher for high skilled workers. In addition, the gap between the marginal product and the expected wage o olers increases for occupations with higher education costs. This gap is exactly what A cemoglu and Pischke (1999) define as a compressed wage structure.

The paper preceeds as follows. The framework of the model is laid out in section 2. Section 3 derives the main result on the positive correlation of wages across occupations within a firm and characterises the labor market equilibrium as well as the wage o $\square$ er distributions for each occupation. Section 4 links the
wage oner distributions with the cost of education and analyses the equilibrium occupation decision. Section 5 investigates the impact of search frictions on search rents across occupations and on the shape of the wage distribution.

## 2 The Framework

The model has an infinite horizon and is set in continuous time. The paper concentrates on steady states. Each worker of the measure p of ex-ante identical workers joins one of two occupations I = $1>2$ before he starts to search for a job in the labor market. The measure of each occupation I is defined as $t_{1}$, satisfying $t_{1}+t_{2}=p$. The measure $x_{1}$ of workers is unemployed and the measure $t_{1} \square x_{1}$ is employed. At a rate $\square A 0$, a worker leaves the labor market and is replaced by a young worker, who has to choose an occupation before he enters the labor market as unemployed. Workers incur a oneol cost $f_{l}$ for occupation specific education. By assuming perfect capital and insurance markets, workers are able to borrow the cost of education before they start to earn money. They pay the interest rate $\square$ on the cost of education due to their uncertain life span. Workers are assumed to be risk neutral and hence join the occupation with the highest expected value of being unemployed.

After joining an occupation workers search for a job in the separated labor markets of their occupation. They follow a sequential search strategy, i.e. they sample only one job o $\square$ er and decide whether or not to accept it. With probability $\square_{x}$ unemployed workers encounter a firm that makes them a wage oDer corresponding to their occupation, and with probability $\square_{\mathrm{n}}$ employed workers encounter a firm. The arrival rate of o[ers across occupations is assumed to be constant.

The measure of ex-ante identical firms is normalised to 1 . All firms have the same production technology $\mid=\backslash\left(q>_{2}\right)$ where $Q\left(z_{1} \mid z_{1}^{\mu} ⿻_{1}\left(z_{1}\right)\right)$ is the
occupation size of a firm that oПers wage $z_{1}$, given the reservation wage $z_{1}^{\mu}$ and the wage o $\square$ er distribution $I_{\|}\left(z_{1}\right)$. The production function exhibits diminishing marginal returns, i.e. $Q(q>0) @ C Q A 0, C^{2} \backslash(q>0) @_{C} q^{2} ? 0$, has a positive cross derivative, i.e. $C^{2} \backslash\left(Q>O_{2}\right) @ C_{a} C O A$, and satisfies the Inada conditions. For the derivation of the explicit wage o oler distribtion is the additional assumption of constant returns to scale necessary. Firms maximize profits by o $\square$ ering a wage schedule $\left(z_{1} \boldsymbol{Z}_{2}\right)$.

## 3 Labor M arket Equilibrium

### 3.1 W orkers' optimal search strategy

The optimal search strategy for a worker of occupation I depends on the reservation wage $\mathbf{z}^{\mu}$, where the unemployed worker is indi■erent between accepting or rejecting a wage o $\square$ er, i.e. $X_{I}=Y_{I}\left(z_{l}{ }^{\mu}\right)$, where $X_{I}$ is the value of being unemployed and $Y_{l}\left(z_{l}^{\mu}\right)$ the value of being employed at the reservation wage $z_{l}^{\mu}$. Wage oПers below the reservation wage have no value to the worker. For wage o $\square$ ers above the reservation wage, the Belmann equation is ${ }^{1}$

$$
\square X_{1}=\square_{z_{1}^{u}}^{Z_{1}}\left(Y _ { 1 } ( \{ _ { 1 } ) \square X _ { 1 } ) g l _ { 1 } \left(\left\{_{1}\right) \square \square f_{1},\right.\right.
$$

where $I_{I}\left(\left\{_{I}\right)\right.$ is the wage oПer distribution for occupation $I$ and $\bar{z}_{I}$ the supremum wage o $\square$ ered for occupation I. It says that the flow value of being unemployed equals the expected gain from changing from unemployment to emploment minus the interest payment on the cost of education,

The flow value of being employed at wage $z_{1}$ is given by

$$
\square Y_{1}\left(z_{1}\right)=z_{1}+\square_{n}^{Z_{l}}\left(Y _ { 1 } ( \{ _ { 1 } ) \square Y _ { l } ( z _ { 1 } ) ) g l _ { l } \left(\left\{_{1}\right) \square \square f_{1} .\right.\right.
$$

[^1]If an employed worker is o olered his current wage, he is indi $\square$ erent between changing employer or not. Thus his current wage is also his reservation wage. Evaluating equation (2) at the reservation wage and subtracting (2) from (1) as well as integrating the resulting equation by parts gives the reservation wage equation,
which gives the minimum wage for which an unemployed person is willing to accept a job. Due to the fact that workers' education cost is sunk at the time they enter the labor market (hold-up problem), the cost of education does not $a \square$ ect their labor market decision on whether or not to accept an o $\square$ ered wage.

### 3.2 Steady state flows and occupation size

Given the reservation wage one can easily construct the steady state measure $\mathrm{x}_{\text {I }}$ of unemployed workers. The outflow of unemployment is given by the measure of unemployed $x_{1}$ multiplied by the probability of receiving an o $\square_{\mathrm{e}} \square_{x}$ and the proportion of workers who accept the wage o $\square$ er $1 \square I_{I}\left(z_{\|}^{\mu}\right)$ as well as the flow of workers retiring $\llbracket x_{1}$. The inflow into unemployment is given by the measure of young workers entering the labor market, which is equal to the flow of workers $\square t_{1}$ leaving each occupation. Thus the steady state measure of unemployed is given by

$$
\begin{equation*}
x_{1}=\frac{\Pi_{1}}{\square+\square_{x}\left(1 \square I_{1}\left(z_{1}^{u}\right)\right)} . \tag{4}
\end{equation*}
$$

Now we define $J_{।}\left(z_{\|}\right)$as the cumulative wage earnings distribution, that is the proportion of employed workers of occupation I, who earn a wage less or equal to $z_{1}$. Then the measure of workers who earn $z_{1}$ or less is given by $J_{1}\left(z_{1}\right)\left(t_{1} \square x_{1}\right)$. The inflow into this group out of unemployment $x_{1}$ is given by the probability $\square_{x}\left(I_{I}\left(z_{\mid}\right) \square I_{I}\left(z_{\mid}^{\prime}\right)\right)$ of receiving and accepting wage o $\square$ ers up to
 retire at rate $\square$ or they receive a higher wage o oner from another firm, which occurs at rate $\square_{h}$, and accept it, which happens with probability (1]I।( $\left.z_{l}\right)$ ). Equating the inflow and outflow gives the steady-state measure of employed workers earning a wage not greater than $\mathrm{z}_{\mathrm{I}}$.

$$
\begin{equation*}
J_{I}\left(z_{1}\right)\left(t_{1} \square x_{1}\right)=\frac{\square_{x}\left(I_{1}\left(z_{1}\right) \square I_{1}\left(z_{1}^{u}\right)\right)}{\left(\square+\square_{h}\left(1 \square I_{1}\left(z_{1}\right)\right)\right)\left(\square+\square_{x}\left(1 \square I_{1}\left(z_{1}^{u}\right)\right)\right)} \square t_{1} \tag{5}
\end{equation*}
$$

The next step is to derive the steady-state occupation size per firm. From (5) it follows that the measure of workers in occupation I earning a wage in
 $I_{\|}\left(z_{1}\right) \square I_{1}\left(z_{I} \square \$_{\phi}\right.$ is the measure of firms o $\square$ ering a wage in the same interval. Hence, the occupation size per firm is given by the measure of workers earning wage $z_{\text {। }}$ divided by the measure of firms o ering $z_{1}$.

$$
Q\left(z_{1} \mid z_{1}^{u} x_{1}\left(z_{1}\right)\right)=\lim _{\%<0} \frac{J_{1}\left(z_{1}\right) \square J_{1}\left(z_{1} \square \mathscr{O}_{1}\right.}{I_{1}\left(z_{1}\right) \square I_{1}\left(z_{1}\right] \mathscr{\phi}}\left(t_{1} \square x_{1}\right)
$$

Therefore, the steady-state occupation size available to a firm oПering a particular wage can be expressed as


$$
I_{1}\left(z_{1}\right)=I_{1}\left(z_{1}^{3}\right)+\left(z_{1}\right)
$$

given $\left(z_{1}\right)$ is the mass of firms o olering $z_{1}$. From (6) it follows that the occupation size $Q\left(z_{\mid} \mid z_{1}^{\mu} \boldsymbol{x}_{1}\left(z_{1}\right)\right)$ (for $\left.z_{\mid} \square z_{\mid}^{\mu}\right)$ is (i) increasing in $z_{1}$; (ii) continuous except where $I\left(z_{I}\right)$ has a mass point; and (iii) strictly increasing on the support of $I_{1}\left(z_{1}\right)$ and a constant on any connected interval o $\square \square$ the support of $I_{\text {I }}\left(Z_{1}\right)$.
3.3 Firms' profit maximization problem

Firms take workers' on-the-job search strategy as well as the size of the occupations $t_{1}$ as given. Each firm posts a wage schedule ( $z_{1}>_{2}$ ) in order to maximize its profit, conditional on $z_{1}^{u}$ and $I_{I}\left(z_{I}\right)$.

$$
\begin{equation*}
\left.\left.\square\left(z_{1} z_{2}\right)=\max _{\left(z_{1} z_{2}\right)}\left[\backslash\left(q z_{2}\right)\right] z_{1} Q\right] z_{2} \theta\right] \tag{7}
\end{equation*}
$$

where $Q\left(z_{\mid} \mid z_{\mid}^{\mu} \boldsymbol{x}_{1}\left(z_{1}\right)\right)$ is the occupation size per firm defined by equation (6).
3.4 Equilibrium solution to wage posting game

The labor market equilibrium consists of a single profit $\square$ and a combination $\left(z_{1}{ }_{1} \boldsymbol{X}_{1}\left(z_{1}\right)\right)$ for each occupation I such that unemployed workers follow their optimal search strategy, characterised by (3). Firms maximize their profits by oПering a wage schedule ( $z_{1}>z_{2}$ ) such that the first and second order conditions are satisfied, and $I_{I}\left(z_{1}\right)$ for all $I=1 \geqslant 2$ is such that

$$
\begin{align*}
& \square=\backslash\left(q>O_{2}\right) \square z_{1} Q \square z_{2} O_{2} \text { for all } z_{\text {I }} \text { on the support of } I\left(z_{1}\right)  \tag{8}\\
& \square \square\left(q>O_{2}\right) \square z_{1} Q \square z_{2} O_{2} \quad \text { otherwise. }
\end{align*}
$$

Let $w_{\mid}$and $\bar{z}_{\mid}$denote the infimum and supremum of the support of an equilibrium wage distribution $I_{I}\left(z_{1}\right)$. Since no worker would accept a wage below his reservation wage, o■ering a wage below the reservation wage would imply zero profits. Without the loss of generality, we therefore only consider distribution functions that satisfy $w_{m} \square z_{m}^{u}$

Lemma 1 The wage o $\square$ er distributions are continuous.
Proof: See appendix.
The basic argument is given by Burdett and M ortensen (1998). If all firms o $\square$ er the same wage for one occupation, then by o■ering a slightly higher wage a firm could attract a significantly larger steady-state occupation size.

This wage increase can be arbitrarily small, whereas the resulting increase in occupation size is significant, since all workers currently working for the mass point wage will change to the new employer as soon as they get this higher wage o oler. This generates a higher profit for the firm since the increase in total output due to the significantly larger workforce is higher than the increase in total cost induced by this slight wage increase. Thus, firms find it profitable to deviate from a mass point by o olering a slightly higher wage. Thus no mass point exists. The resulting labor supply curve a single firm faces is upward sloping, since a higher wage $z_{\text {I }}$ attracts more workers and reduces turnover and thus leads to a larger steady-state occupation size for this firm.

The firm o■ering the lowest wage maximizes its profit if and only if it o■ers the reservation wage, i.e. $w_{I}=z_{1}^{\mu}$. Lemma 1 implies that $I_{I}\left(z_{I}\right)$ is continuous for $w_{1} \square z_{1}^{\mu}$, and that the occupation size of a firm posting the wage $z_{\text {I }}$ can be expressed as

$$
\begin{equation*}
Q\left(z_{1} \mid z_{1}^{u} x_{1}\left(z_{1}\right)\right)=\frac{\left.\square\left(\square+\square_{h}\right) @ \square+\square_{x}\right)}{\left[\square+\square_{h}\left(1 \square I_{1}\left(z_{1}\right)\right)\right]^{2}} t_{l} \tag{9}
\end{equation*}
$$

since $I_{I}\left(Z_{\mid}^{\mu}\right)=0$. Note again that the occupation size is increasing in the posted wage, since firms o■ering higher wages attract more workers and reduce turnover.

Proposition 1 Firms' profit maximization behavior ensure that firms occupy the same position in the wage distribution for both occupations. This is the so called k-percent rule $I_{1} z_{1}^{n^{\phi}}=I_{2} i_{2} n^{\phi}$.

P roof. Profit maximization puts certain restrictions on the cross-occupation relation between wages and occupation size. The first order condition of the profit maximization problem (7) for both occupations is

$$
\frac{Q \square\left(z_{1}>z_{2}\right)}{C z_{1}}=\frac{Q}{C Q} \frac{C Q}{C z_{1}} \square z_{1} \frac{C Q}{C z_{1}} \square Q=0 .
$$

We now introduce an index $n$, which orders the firms as they increase their wage o must hold for any wage schedule posted on the support of both wage o $\square$ er distributions $I_{1}\left(z_{1}\right)$. Thus, the total derivative of the first order condition has to be zero, which implies that

$$
\frac{g z_{1}^{n}}{g z_{2}^{n}}=\square \frac{\frac{C^{2} \square\left(z_{1}>z_{2}\right)}{C z_{2}^{2}}}{\frac{C^{2} \square\left(z_{1}>z_{2}\right)}{C z_{1} C z_{2}}} .
$$

Since the size of occupation I does not depend on the wage of other occupations, (i.e. $\left.C_{0} @ z_{1}=0\right)$ as can be seen from equation (9), and since the occupations are assumed to be complements, it follows that the cross derivatives are positive

$$
\frac{\mathrm{C}^{2} \square\left(z_{1} z_{2}\right)}{\mathrm{C}_{1} C z_{2}}=\frac{C^{2} \backslash}{C Q C_{2}} \frac{C q}{C z_{1}} \frac{C_{2}}{C z_{2}} A 0 .
$$

For a maximum the Hessian matrix has to be negative semi-definite. Hence, the second derivative has to be non-positive, i.e.

$$
\frac{C^{2} \square\left(z_{1}>z_{2}\right)}{G_{1}^{2}} 60 .
$$

The continuity result of lemma 1 implies that the second derivatives are strictly negative, since it rules out $g z{ }_{1}^{n} @ z{ }_{2}^{n}=0$. Thus firm $n$, which posts a higher wage for occupation 1 than firm $\mathrm{n} \square 1$, also posts a higher wage for occupation
2. Since the relationship $g z{ }_{1}^{n} @ z{ }_{2}^{n}$ is continuous due to the continuity of the derivatives, it implies that the proportion of firms $I_{1} Z_{1}^{n}{ }^{\dagger}$ o 0 ering a wage no greater than $z_{1}^{n}$ is the same as the proportion of firms $I_{2} z_{2}^{n}{ }^{\Phi}$ o obering a wage no greater than $z{ }_{2}^{n}$. Since these wages are set by the same firm $n$, it follows that $I_{1}{ }^{i} z_{1}^{n^{\Phi}}=I_{2}{ }^{i} z_{2}^{n}$.

Each firm occupies the same position in the wage distribution for all occupations because each single firm faces an upward sloping labor supply curve for
each occupation and in addition, because the cross derivative of the production function is assumed to be positive; this means that the two occupations are complements. ${ }^{2}$ Thus, the cheapest way to increase output is to increase the size of both occupations simultaneously, which can only be done by increasing both wages simultaneously. The complementarity implies that it is optimal to increase the output along the support of both wage-o $\square$ er distributions $I_{I}\left(z_{1}\right)$.

This positive correlation between the wages of workers in di■erent occupations within a single firm is well established empirically. B arth and Dale-OIsen (2003) find that "[h]igh-wage establishments for workers with higher education are high-wage establishments for workers with lower education as well".

The k-percent rule derived in proposition 1 also implies that one firm oПers the reservation wage for all occupations. The equilibrium condition (8) defines the isoprofit curve that the firms have to be on. In particular the firm o olering the reservation wage to both occupations must also earn the equilibrium profit,
 the example of firm $n$ o■ering a wage schedule above the reservation wage. The k-percent rule, $I_{1} z_{1}^{n^{\Phi}}=I_{2} i_{2}^{n}{ }^{\Phi}$ and the constant return to scale assumption allows for $I_{1}{ }^{i} z_{1}{ }^{\Phi}$ to be factored out. Since this holds for any $n$, the index can be dropped. Using the equilibrium condition, i.e. $\square^{u}=\square$, and rearranging, gives:
for both occupations. The following proposition solves for $I_{I}\left(z_{I}\right)$ as a function of solely $z_{1}$ and not of $Z_{m}$

[^2]Proposition 2 The closed form solutions for the unique wage o $\square$ er distributions for each occupation $I=1>2$ is given by

$$
\begin{equation*}
I_{1}\left(z_{1}\right)=\frac{\square+\square h}{\square_{h}} 1 \square \frac{\tilde{A}}{\frac{\mathrm{C}\left(t_{1} \not \star_{2}\right) @ t_{1} \square z_{1}}{\mathrm{Q}\left(\mathrm{t}_{1} \star_{2}\right) @ t_{1} \square \mathrm{z}_{1}^{u}}} . \tag{11}
\end{equation*}
$$

Proof: See appendix.
The explicit wage o $\square$ er distribution for each single occupation resembles the distribution derived by Burdett and Mortensen (1998). The single wage o oler distributions depend on the occupation-specific marginal product. Thus all occupations are linked by the production function. ${ }^{3}$

W ith the closed form solution for the wage o■er distribution it is easy to calculate the reservation wage:

$$
\begin{equation*}
z_{1}^{u}=\frac{\left(\square_{x} \square \square_{n}\right) Q\left(t_{1} \star_{2}\right) @ t_{1}}{\square+\square_{x}} . \tag{12}
\end{equation*}
$$

The occupation specific supremum wage can be derived from $I_{I}\left(\bar{Z}_{I}\right)=1$.

## 4 Equilibrium Occupation Decision

Young individuals replace the retired. Before they enter the labor market as unemployed they have to choose an occupation. Since they are risk neutral, young workers compare the flow value of being unemployed across occupations and join the occupation with the highest expected value. Thus, in equilibrium all occupations must promise the same expected value of being unemployed.

Given the reservation wages and the wage-oПer distributions, it is easy to compare the flow value of being unemployed across occupations. The value of

[^3]being unemployed (4) can be written as follows
\[

$$
\begin{align*}
\square X_{1}\left(t_{1}\right) & =\square_{x}^{Z_{1} \mu} \frac{1 \square I_{1}\left(\left\{_{1}\right)\right.}{\square+\square_{n}\left(1 \square I_{1}\left(\left\{_{1}\right)\right)\right.} \text { ी } g\left\{_{1} \square \square f_{1}\right.  \tag{13}\\
& =\frac{\square_{x}}{\square+\square_{x}} \frac{Q\left(t_{1} \star_{2}\right)}{C t_{1}} \square f_{1}
\end{align*}
$$
\]

for all $1=1 \geqslant 2$.
The equilibrium occupation decision is given by an equilibrium in the labor market and a common value of being unemployed $X$ as well as proportions

i) $\quad X_{1}\left(t_{1}\right)=X$ for all $t_{1}=t_{1}^{W}$ $X_{1}\left(t_{1}\right) \square X$ for all $t_{1} \in t_{1}^{w}$
ii) $\quad t_{1}^{W}+t_{2}^{W}=p$
iii) $\quad \mathrm{t}_{1}^{\mathrm{W}} \mathrm{A} 0$ for all I = $1 \geqslant 2$.

Proposition 3 There exists a unique equilibrium occupation decision that maximises the equilibrium unemployment value $X$ but encourages too few individuals to choose the high cost occupation compared with the first best.

Proof: see appendix.
The fact that young workers aim for the occupation with the highest marginal product and the diminishing marginal rate of return for a single occupation implies that the marginal products adjust to equate the values of unemployment across occupations. The positive cross derivatives guarantee that the equilibrium value has a unique maximum.

The marginal products adjust to compensate the young worker in expected terms for the cost of education $f_{l}$ but also for losses in the expected unemployment period

$$
\begin{equation*}
\square\left(f_{1} \square f_{2}\right)=\frac{\square}{x}_{\square+\square_{x}}^{\mu} \frac{\mathrm{Q}\left(\mathrm{t}_{1} \star_{2}\right)}{\mathrm{Ct}_{1}} \square \frac{\mathrm{Q}\left(\mathrm{t}_{1} \star_{2}\right)}{\mathrm{Ct}_{2}} \tag{14}
\end{equation*}
$$

Thus the di $\square$ erence between the marginal products is higher than in a world without frictions. Put diПerently fewer individuals than in a first best competitive environment are willing to choose the occupation with a higher cost of education. If labor market frictions vanish, i.e. $\square_{x} \$ 4$, unemployment spells become negligible and thus the reservation wage converges to the marginal product. This implies that the wage distribution collapses to a mass point at the marginal product, which induces a first best education investment.

## 5 Search Frictions, Rents and the Shape of the Wage Distribution

### 5.1 Search rents and the compression of wages

Firms make positive profits as shown in the labor market equilibrium of section
3. Given that firms pay a wage below the marginal product, the question arises whether firms extract more search rent from occupations with a high cost of education or occupations with a low cost of education. We define the search rent going to the firm as the gap between the marginal product and the expected earnings of a worker in occuaption I. The occupation-specific earnings distribution can be derived from the wage o $\square$ er distribution by using equations (4) and (5).

Proposition 4 Firms extract more search rent from workers with a higher marginal product, i.e. from workers with higher education.

Proof. Integration and substitution of $\bar{z}_{\mid}$and $z_{\mid}{ }^{\mu}$ gives:

Thus, $\mathrm{V}_{\mathrm{l}}$ increases with the marginal product.
Search frictions prevent workers from obtaining the full marginal product. The surplus of the expected match, i.e. the marginal product, is split according to the (un)employment rate. Workers get the expected proportion equivalent to the employment rate, which equals the value of being unemployed not considering the sunk cost of education. Firms get the fraction equal to the unemployment rate $x_{1}$. Since unemployment and employment rates - that determine the split - are constant across occupations, firms extract more rent from the occupation with the higher marginal product and thus the higher cost of education.

A cemoglu and Pischke (1999) define a wage structure as compressed if the gap between the marginal product and the expected wage o■er rises for occupations with higher education cost. They argue that search and bargaining in a Pissarides environment leads to a compressed wage structure. Wage posting in an on-the-job search model can lead to a similar structure as stated in the following proposition.

Proposition 5 W ages of higher educated workers are more compressed than wages of lower educated workers.

Proof. Integration and substitution of $\bar{z}_{\mid}$and $z_{1}^{u}$ gives:

$$
F_{1}={ }_{z_{1}^{u}}^{\bar{z}_{1} \mu^{u}} \frac{Q\left(t_{1} x_{2}\right)}{a_{1}} \square z_{\mid} g_{1}\left(z_{1}\right)=\frac{1}{3} \frac{\left(\square+\square_{h}\right)^{3} \square \square^{3}}{\square_{n}\left(\square+\square_{h}\right)\left(\square+\square_{x}\right)} \frac{Q\left(t_{1} x_{2}\right)}{C_{1}}
$$

Thus, $F_{1}$ increases with the marginal product and hence for workers with higher education cost.

Wage compression occurs if future employers are not able to extract the same rent from workers than the current employer. The simple fact that only a higher wage than the current wage induces a worker to change his employer
implies that future employers can extract less search rent than the current employer. Since a firm's search rent is higher for higher educated workers, wage compression also increases with education.

The gap between the marginal product and the expected wage o $\square$ ers only closes if wage o olers for unemployed arrive at an infinite rate. A higher o■er arrival rate of employed workers leads to a higher wage compression, because recruitment of employed workers becomes easier and o■ering a higher wages to attract more employed workers becomes therefore less attractive. The wage oПer distribution is therefore less steep leading to more compressed wage structure.
5.2 The shape of the wage o $\square$ er and earnings distribution

The following section presents a simulation exercise based on a Cobb-Douglas productions function with five occupations, which di $\square$ er in the cost of education. A ssumed exogenously are the production factor $s=500$, the population size $p=50$, unemployment benefits $e=50$, the arrival rates $\square_{x}=0 \pm 5$ and $\square_{h}=0 \oplus 8$, the separation rate $\square=0 \not \theta 2$ as well as the cost of education $f_{l}$ and the production elasticites $\square_{1}$. A natural assumption supported by many empirical studies is to let the production elasticity decrease while the cost of education increases (for a summary of the literature see Hamermesh 1996, chapter 3). The production function has the following form:

$$
\backslash(I)=S_{l=1}^{Y^{5}} Q\left(z_{\mid} \mid z_{l}^{u} x_{l}\left(z_{\mid}\right)\right)^{\square_{l}}
$$

where I represents the vector of the five occupation sizes $Q\left(z_{l}\left|z_{1}^{u}\right\rangle_{l}\left(z_{1}\right)\right)$.
Table 1 presents the equilibrium occupation size $t_{1}{ }^{W}$, which is determined endogenously according to section 4. These determine the marginal products Cl @ ${ }_{1}$, which in turn determine the reservation $\mathrm{z}_{1}{ }^{\mathrm{u}}$ and supremum wages $\bar{z}_{\text {I }}$ according to the analysis given in section 3 .

Table 1: Occupation size, reservation and supremum wages

|  | Occupations |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 | 5 |
| Production elasticities $\square_{1}$ | 0.45 | 0.30 | 0.10 | 0.10 | 0.05 |
| Cost of education $\mathrm{f}_{1}$ | 0 | 300 | 700 | 1800 | 3000 |
| Occupation size $\mathrm{t}_{1}{ }^{\text {b }}$ | 25.2 | 15.3 | 4.7 | 4.0 | 1.7 |
| Marginal products Cl @t, | 271.2 | 429.4 | 1379.0 | 1471.4 | 3434.3 |
| Reservation wages $z_{1}^{4}$ | 79.7 | 82.5 | 86.2 | 96.5 | 107.7 |
| Supremum wages $\bar{z}_{1}$ | 120.3 | 127.0 | 135.8 | 160.2 | 186.7 |

The equilibrium occupation-specific, wage-oDer densities are increasing and convex as is the original wage o oler density of the simple Burdett-M ortensen model:

$$
1, q\left(z_{1}\right)=\frac{\square+\square n}{2 \square n} q \frac{1}{\frac{\overline{\overline{t_{1}}} \backslash(q) \square z_{1}^{u}}{q}} q \frac{1}{\overline{\frac{\overline{t_{1}} \backslash(q) ~}{t_{1}}} \frac{1}{z_{1}}} .
$$

The aggregate density across all occupations is the weighted average of the individual densities, where the support of the individual densities starts at the respective reservation wage and ends with the supremum wage at di $\square$ erent points:

$$
I_{\mathrm{djj}}^{0}(z)=\sum_{I=1}^{x^{q}} \frac{t_{1}}{\mathrm{p}} I_{1}\left(z_{1}\right)
$$

Figure 1 presents the simulation with five occupations. The density has five jumps at each occupation's reservation wage and five spikes, one at the supre mum wage of each occupation.


Figure 1: Density of aggregate wage offers

A s the number of occupations increase, the aggregate density function mirrors more and more a right-tailed, wage-o tions also have an increasing convex density, as can be easily verified from the cumulative distribution given in equation (15). Figure 2 shows the aggregate wage-earnings density analogue to Figure 1.


Figure 2: Density of aggregate wage earnings

## 6 Conclusion

This paper's extension of the Burdett-M ortensen (1998) model by introducing two di $\square$ erent occupations provides an explanation for the empirically observed positive correlation between the wages of workers in diDerent occupations within firms. The driving forces are the complementarity of the occupations in the production process and the local monopsony power of each firm that leads to an upward sloping labor supply curve for each occupation.

The result that firms occupy the same position in the wage distribution for each occupation allows us to solve for the explicit occupation-specific, wage o $\square$ er distributions. Although the single, occupation-specific wage distributions have an increasing left-skewed density aggregation over all occupations, a spiky right-tailed density results when assuming that the production elasticities increase for occupations with a lower cost of education.

In the occupation-decision equilibrium, marginal products adjust to account for the di $\square$ erences in the cost of education and the degree of search frictions in the labor market. The dinerences in the marginal products are therefore higher than in a first best competitve environment. This wedge be tween the marginal products increases with the degree of market frictions. In addition, search frictions give each firm some local monopsony power, which the firm uses to extract some rent from its workers. This search rent depends on the degree of labor market frictions and is higher for high skilled workers. In addition, the gap between the marginal product and the expected wage o $\square$ ers increases for occupations with higher education costs. Thus, wages are compressed.

## A ppendix

Proof of Lemma 1:
Recall that $q_{r}\left(z_{m} \mid z_{m}^{u} \psi_{l}\left(z_{n}\right)\right)$ is only discontinuous at $z_{m}=\hat{z}_{m}$ if $\hat{z}_{m}$ is a mass point of $I_{I}\left(z_{m}\right)$ and $\hat{z}_{m} \square z_{m}^{u}$ Suppose there exists a mass point at $Z_{m}=\hat{Z}_{m}$ then by o $\quad$ ering a slightly higher wage than $\hat{Z}_{m}$ a firm could attract a significantly larger steady state labor force for this occupation $m$ This could generate a higher profit if the increase in total output, induced by this slight wage increase, is higher than the increase in total cost. The first thing to notice is that the increase in the wage is insignificant, since $Z_{m}$ is continuous, whereas the increase in the labor force is significant, since $q_{r}\left(z_{m} \mid z_{m}^{u} \|_{1}\left(z_{m}\right)\right.$ is discontinuous at the mass point. It follows that the increase in total cost is $Z_{m}\left\{Q_{n}\right.$ and the increase in total output is

$$
\left\{\mid=\backslash\left(Q>a_{n}+\{Q\}\right\rangle \backslash\left(Q>x_{n}\right) .\right.
$$

Using a first order Taylor-series-expansion around the initial occupation size Qngives

$$
\left\{\left\lvert\,=\frac{C}{C_{n}}\left\{Q_{n}\right.\right.\right.
$$

Therefore, a deviation from the mass point at the wage $z_{m}$ is profitable as long as the marginal product exceed the wage:

$$
\begin{equation*}
\left\{\left\lvert\, \square z_{m} q_{n}=\frac{\mu}{C_{Q}} \square z_{m}^{q}\left\{q_{m} A 0 .\right.\right.\right. \tag{16}
\end{equation*}
$$

Given C @cQ $A Z_{m}$ it is optimal for each firm to deviate from any mass point (i.e. o oler a slightly higher wage). Since it is always possible to increase the wage by $\square$ A 0 such that the wage remains below the marginal product, it follows that no mass point exists. $\mathrm{C} @ \mathrm{@} \mathrm{z}_{\mathrm{m}}$ is a necessary condition for firms to earn positive profits in equilibrium. The existence of an equlibrium
with positive profits (given the Inada conditions) rules out any zero profits equilibrium and hence any equilibrium with mass points. $¥$

## Proof of Proposition 2:

Homogeneity of degree one implies, according to the Euler Theorem:

$$
\backslash\left(q>O_{2}\right)=q Q\left(q>O_{2}\right) @ q+Q_{2} Q\left(q>\theta_{2}\right) @_{2} .
$$

The first order condition implies

$$
\frac{Q}{C Q} Q=z_{1} Q+\frac{Q^{2}}{C Q @ z_{1}} .
$$

Thus, the equal profit condition looks like the following:

Using the wage o $\square$ er distribution with the sum of wage payments (10) it is easy
 support of $I_{I}\left(z_{I}\right)$. Substituting this result back into the equal profit condition, using the homogeneity of degree one property again and rearranging, gives:

$$
\frac{\square\left(q x_{2}\right) @_{Q} \square z_{1}}{\square\left(q^{\prime} x_{2}^{\prime}\right) @ Q^{\prime} \square z_{1}}=\frac{\left[\square+\square_{h}\left(1 \square I_{1}\left(z_{1}\right)\right)\right]^{2}}{\left(\square+\square_{h}\right)^{2}} .
$$

The Euler theorem for a linearly homogenous production function also implies that the first derivatives of the production function are homogenous of degree zero, therefore

$$
\frac{a\left(t_{1} \star_{2}\right) @ t_{1} \square z_{1}}{\mathrm{Q}\left(\mathrm{t}_{1}^{u} \star_{2}^{u}\right) @ t_{1}^{u} \square z_{1}}=\frac{\left[\square+\square_{n}\left(1 \square I_{1}\left(z_{1}\right)\right)\right]^{2}}{\left(\square+\square_{n}\right)^{2}} .
$$

Rearranging gives the equilibrium wage o $\square$ er distribution (11). $¥$

The FOC and SOC hold with the equilibrium $I_{1}\left(z_{1}\right)$, proof:
First order condition:

$$
\frac{\mathrm{Q} \square\left(z_{1} z_{2}\right)}{\mathrm{C} z_{1}}=\frac{\mu \mathrm{Q}}{\mathrm{CQ}} \square z_{1} \frac{\mathrm{CQ}}{\mathrm{Cl}_{1}\left(z_{1}\right)} I_{1} q_{\left.z_{1}\right) \square Q}^{Q}
$$

Using the fact that

$$
\frac{2 \square_{n} 1{ }_{1}\left(z_{1}\right)}{\left[\square+\square_{h}\left(1 \square I_{1}\left(z_{1}\right)\right)\right]}=\frac{1}{\left(\mathrm{C}\left(t_{1} x_{2}\right) @ t_{1} \square z_{1}\right)}
$$

and the homogeneity of degree zero property of the first derivative of the production function shows

Second order condition:
Define: $\square_{ı} \square \frac{C^{2} \square\left(z_{1} \not z_{2}\right)}{C z_{1}^{2}}$ and $\square_{1 m} \square \frac{C^{2} \square\left(z_{1} \not z_{2}\right)}{C z_{1} C z_{m}}$
For the Hessian matrix to be negative semi-definite, it has to be the case that (i) $\square_{ı}$ ? 0 and that the determinant of the $(2 \times 2)$ Hessian matrix has to be non-negative, (ii) $\square_{11} \square_{22} \square \square_{12} \square_{21}>0$. The second derivative is given by:

Using the first order condition to substitute $C @ \square \square z_{\text {I }}$ out and recognizing after some calculations that

$$
\frac{C^{2} Q}{C_{1}^{2}}=2 \frac{C Q}{C Z_{1}} \frac{C Q}{C_{1}} \frac{1}{Q}
$$

gives (i)

$$
\frac{C^{2} \square\left(z_{1}>z_{2}\right)}{C_{1}^{2}}={\frac{C^{2}}{C^{2}}}^{\mu}{\frac{C Q}{C z_{1}}}^{\mathrm{q}_{2}} ? 0
$$

The E uler theorem for a linearly homogenous production function also implies that the first derivatives of the production function are homogenous of degree zero, i.e.

$$
q^{C^{2} \backslash} \frac{C^{2}}{C^{2}} \frac{C^{2} \backslash}{C q C_{2}}=Q_{2} \frac{C^{2} \backslash}{C_{9}^{2}}+a \frac{C^{2} \backslash}{C q C O}=0,
$$

which implies:
$\nexists$

Proof of Proposition 3:
In the occupation decision equilibrium the two values of being unemployed (13) have to be equal, hence

$$
\square\left(f_{1} \square f_{2}\right)=\frac{\square_{x}}{\square+\square_{x}} \frac{}{\mu}_{Q_{\left(t_{1} \star_{2}\right)}^{C t_{1}} \square \frac{Q\left(t_{1} \star_{2}\right)}{\mathrm{Ct}_{2}} .} .
$$

This defines the implicit function $t_{1}\left(t_{2}\right)$. The implicit function theorem implies:

$$
\frac{g t_{1}}{g t_{2}}=\frac{\frac{C^{2} \backslash\left(t_{1} \star_{2}\right)}{\mathrm{Ct}_{2} C t_{1}} \square \frac{C^{2} \backslash\left(t_{1} \star_{2}\right)}{{C t_{2}^{2}}_{C^{2} \backslash\left(t_{1} \star_{2}\right)}^{\mathrm{Ct}_{2} \mathrm{Ct}_{1}}} \square \frac{C^{2} \backslash\left(t_{1} \star_{2}\right)}{\mathrm{Ct}_{1}^{2}}}{A} .
$$

Hence $t_{n}\left(t_{1}\right)$ is an increasing function with domain and range ( $0>4$ ). The occupation decision equilibrium also requires that summation condition $t_{1}+$ $t_{2}=p$ holds. The summation condition defines a decreasing function $t_{1}\left(t_{2}\right)$
 with $t_{1}^{W} \mathrm{~A} 0$ and $\mathrm{t}_{2}^{\mathrm{w}} \mathrm{A} 0$.

Note also, that for $\square_{x}$ ? 4 the di $\square$ erence in the marginal products are larger than compared with an environment without frictions, i.e. $\square_{x} \$ 4 . \neq$

## R eferences

A cemoglu D. and J.-S. Pischke, (1999), "The Structure of Wages and Investment in General Training", J ournal of Political Economy 107, 539-572. Albrecht J.W. and B. Axell, (1984), "A n Equilibrium M odel of Search Unemployment", J ournal of Political Economy 92, 812-840.

Barth E. and H. Dale Olsen, (2002), "E mployer Size or Skill-Group Size E Dect on Wages", mimeo, Institute for Social Research, Norway.

Barth E. and H. Dale Olsen, (2003), "Assortative Matching in the Labour M arket", mimeo, Institute for Social Research, Norway.

Bontemps C., J.-M . R obin and G.J . van den Berg, (2000), "E quilibrium Search with Productivity Dispersion: Theory and Estimation", International Economic Review 41, 305-358.

Burdett K. and D.T. Mortensen, (1998), "Wage Di $\square$ erentials, Employer Size and Unemployment", International Economic Review 39, 257-273.

Hamermesh D. S., (1996), Labor Demand, Princeton, New Jersey, Princeton University Press.

K atz L. and L. Summers, (1989), "Industry Rents: Evidence and Implications", Brooklings Papers on Economic Activity: Microeconomics, 209-275.

K iefer N.M . and G.R. Neumann, (1993), "Wage Dispersion with Homogeneity: The Empirical Equilibrium Search Model", in H. Bunzel et al., eds., Panel Data and labor market analysis, Amsterdam: North Holland.
K oning P., G. Ridder and G.J . van den Berg, (1995), "Structural and Frictional Unemployment in an Equilibrium Search Model with Heterogeneous A gents", J ournal of A pplied Economics 105, 133-151.

K remer M., (1993), "The O-ring Theory of Economic Development", Quarterly J ournal of Economics 108 (August), 551-575.
M ortensen D.T., (1990), "Equilibrium Wage Distribution: a Synthesis", in J.

Hartog et al., eds. P anel Data and Labor M arket Studies , A msterdam: North Holland.

M ortensen D.T . and G.R. Neuman, (1988), "Estimating Structural M odels of Unemployment and J ob Duration", in W.A., Barnett et al., eds., Dynamic Econometric M odelling, Proceedings of the Third International Symposium in E conomic Theory and E conometrica C ambridge: Cambridge University Press. van den Berg G.J. and G. Ridder, (1993), "On the Estimation of Equilibrium Search Models with Panel Data", in van Ours J.C. et al., eds. Labor Market Demand and Equilibrium Wage Formation, A msterdam: North Holland. van den Berg G.J. and G. Ridder, (1998), "An Empirical Equilibrium Search M odel of the Labor Market", E conometrica 66, 1183-1221.

## ifo Diskussionsbeiträge

Nr. 1 Thanner, B., Nationale Währungspolitik der sowjetischen Republiken. Ausweg aus der Transformationskrise oder neue Komplikationen?, Oktober 1991.

Nr. 2 Stock, W.G., Wirtschaftsinformationen aus Online-Datenbanken, Dezember 1991.

Nr. 3 Oppenländer, K.H., Erfahrungen in Westdeutschland beim Übergang zur Marktwirtschaft in den Jahren 1947 bis 1960, Januar 1992.

Nr. 4 Mathes-Hofmann, J. und W.G. Stock, Die ifo Bibliothek. Elektronische Bibliotheksverwaltung in einer wirtschaftswissenschaftlichen Spezialbibliothek, Mai 1992.

Nr. 5 Sherman, H., W. Leibfritz, E. Mohr, und B. Thanner, Economic Reforms in the Former Soviet Union, July 1992.

Nr. 6 Adler, U., Technikfolgenabschätzung, August 1992.

Nr. 7 Scholz, L., Technikfolgenabschätzung aus der Sicht der empirischen Wirtschaftsforschung, September 1992.

Nr. 8 Hartmann, M., Zur ordnungspolitischen Kontroverse: Wettbewerbspolitik - Industriepolitik, April 1993. (vergriffen)

Nr. 9 Goldrian, G., Zwei Beispiele für Frühindikatoren auf der Basis von qualitativen Daten, Mai 1993.

Nr. 10 Goldrian, G., Erweiterungen und Verbesserungen des Saisonbereinigungsverfahrens ASA-II, Juni 1993.

Nr. 11 Nam, Ch.W., Can the True Expenditure Needs of a Local Government Be Measured?, October 1993.

Nr. 12 Langmantel, E., LFS.MOD - Ein makroökonomisches Modell zur langfristigen Analyse der deutschen Wirtschaft, Dezember 1993.

Nr. 13 Immenga, U., Mergers and Acquisitions between Germany and the United Kingdom: Legal Framework, Ways and Barriers, December 1993.

Nr. 14 Sauer, T., D. Brand, J. Conrad und E. Mohr, Stellungnahme zum Reform- und Stabilisierungsprogramm der russischen Regierung für 1993-1995, Dezember 1993.

Nr. 15 Herrmann, A. and H. Laumer, Internationalization of Competition Policies: Problems and Chances - A German View, January 1994.

Nr. 16 Lehmann, H. and M.E. Schaffer, Productivity, Employment and Labor Demand in Polish Industry in the 1980s: Some Preliminary Results from Enterprise-level Data, June 1994.

Nr. 17 Stock, W., Wissenschaftsevaluation, Die Bewertung wissenschaftlicher Forschung und Lehre, November 1994. (vergriffen)

Nr. 18 Bellmann, L., S. Estrin, H. Lehmann and J. Wadsworth, The Eastern German Labor Market in Transition: Gross Flow Estimates from Panel Data, August 1994.

Nr. 19 Ochel, W., Economic Policy and International Competition in High-Tech Industries The Case of the Semiconductor Industry, September 1994.

Nr. 20 Ochel, W., Wirtschafts- und Technologiepolitik in High-Tech-Industrien, Februar 1995.

Nr. 21 Lehmann, H. and M. Góra, How Divergent is Regional Labour Market Adjustment in Poland?, February 1995.

Nr. 22 Konings, J., H. Lehmann and M.E. Schaffer, Employment Growth, Job Creation and Job Destruction in Polish Industry: 1988-91, February 1995.

Nr. 23 Schalk, H.J. und G. Untiedt, Unterschiedliche regionale Technologien und Konvergenzgeschwindigkeit im neoklassischen Wachstumsmodell, Empirische Befunde für die Verarbeitende Industrie Westdeutschlands 1978-1989, Juni 1995.

Nr. 24 Nam, Ch.W., Selected Problems of Large German Cities in an Enlarged Europe, July 1995.

Nr. 25 Krylov, D.A., Auswirkungen der Energiewirtschaft auf Umwelt und Gesundheit in Rußland, Oktober 1995.

Nr. 26 Oppenländer, K.H., Hat die empirische Wirtschaftsforschung eine Zukunft?, Oktober 1995.

Nr. 27 Nam, Ch.W., China's Recent Economic Growth and Major Spatial Problems Revealed in Its Marketization Process, November 1995.

Nr. 28 Rottmann, H., Innovationsaktivitäten und Unternehmensgröße in Ost- und Westdeutschland, Februar 1996.

Nr. 29 Adler, U., Welchen Nutzen könnte eine weltweite Harmonisierung der sozialen Standards stiften? Towards a global network for social security and mutual partnership, März 1996.

Nr. 30 Rottmann, H. und M. Ruschinski, Beschäftigungswirkungen des technischen Fortschritts. Eine Paneldaten-Analyse für Unternehmen des Verarbeitenden Gewerbes in Deutschland, Mai 1996.

Nr. 31 Goldrian, G. und B. Lehne, Frühzeitige Erkennung eines Wendepunkts in der konjunkturellen Bewegung einer saisonbereinigten Zeitreihe, November 1996.

Nr. 32 Poser, J.A., A Microeconomic Explanation for the Macroeconomic Effects of InterEnterprise Arrears in Post-Soviet Economies, November 1996.

Nr. 33 Nam, Ch.W. and K.Y. Nam, Recent Industrial Growth and Specialization in Selected Asian Countries, December 1996.

Nr. 34 Paasi, M., Innovation Systems of the Transition Countries - further Restructuring in favour of the Business Sector is necessary, December 1996.

Nr. 35 Scholz, L., The Think Tank Landscape in Germany: A Look Behind the Mirror, January 1997.

Nr. 36 Goldrian, G. und B. Lehne, Ein Vergleich der direkten Schätzung der Konjunkturentwicklung mit einem Verfahren zur Erkennung von Wendepunkten, März 1997.

Nr. 37 Leiprecht, I., Who leaves the agricultural sector? Uncovering hidden flows in agricultural employment in the process of transition in Poland, March 1997.

Nr. 38 Tewari, M., The Role of the State in Shaping the Conditions of Accumulation in India's Industrial Regime: The case of Ludhiana's metal manufacturing sector, May 1997. (vergriffen)

Nr. 39 Tewari, M., Subcontracting Relations and the Geography of Production: a comparative study of four large assemblers in an emerging market, July 1997. (vergriffen)

Nr. 40 Rottmann, H. and M. Ruschinski, The Labour Demand and the Innovation Behaviour of Firms. An Empirical Investigation for West-German Manufacturing Firms, May 1997.

Nr. 41 Poser, J.A., Monetary Disruptions and the Emergence of Barter in FSU Economies, July 1997.

Nr. 42 Poser, J.A., Modelling Barter and Demonetisation in FSU Economies, August 1997.

Nr. 43 Ochel, W., European Economic and Monetary Union and Employment, September 1997.

Nr. 44 Notkin, M., Ausländische Direktinvestitionen in der Russischen Föderation unter besonderer Berücksichtigung des regionalen Aspekts, Oktober 1997.

Nr. 45 Fóti, K., On the Roots of Regional Labour Diversification in Hungary and its Manifestation in the Example of two Hungarian Regions, December 1997.

Nr. 46 Leiprecht, I., Labour Market Adjustment of Agricultural Employment with Special Reference to Regional Diversity, December 1997.

Nr. 47 Köllö, J. and K. Fazekas, Regional Wage Curves in the Quasi-Experimental Stetting of Transition - The Case of Hungary 1986-95, December 1997.

Nr. 48 Góra, M. and U. Sztanderska, Regional Differences in Labour Market Adjustment in Poland: Earrings, Unemployment Flows and Rates, December 1997.

Nr. 49 Klein, Ph.A., Recent U.S. Work in Cyclical Indicators: An Assessment, December 1997.

# Nr. 50 Hoesch, D., Foreign Direct Investment in Central and Eastern Europe: Do Mainly Small Firms Invest?, February 1998. 

Nr. 51 Plötscher, C., Credit Availability and the Role of Relationship Lending, March 1998.

Nr. 52 Juchems, A., Dollarkurs: Schätzung und Prognose, April 1998.

Nr. 53 Plötscher, C. and H. Rottmann:, Investment Behavior and Financing Constraints in German Manufacturing and Construction Firms. A Bivariate Ordered Probit Estimation, May 1998.

Nr. 54 Leiprecht, I., Poverty and Income Adjustment in the Russian Federation, May 1998.

Nr. 55 Starodubrovsky, V.G., The Labour Market and State and Private Enterprises in Russia's Regions, June 1998.

Nr. 56 Lehmann, H., J. Wadsworth, and A. Acquisti, Grime and Punishment: Job Insecurity and Wage Arrears in the Russian Federation, June 1998.

Nr. 57 Adler, U., Social Innovation in the Economic Context: From Evaluation to the Development of Criteria and Models of Good Practise of Healthy Companies, July 1998.

Nr. 58 Goldrian, G., Zur Verdeutlichung der aktuellen konjunkturellen Aussage einer wirtschaftlichen Zeitreihe, Juli 1998.

Nr. 59 Flaig, G. und H. Rottmann, Faktorpreise, technischer Fortschritt und Beschäftigung. Eine empirische Analyse für das westdeutsche Verarbeitende Gewerbe, August 1998.

Nr. 60 Clostermann, J. und F. Seitz, Der Zusammenhang zwischen Geldmenge, Output und Preisen in Deutschland - ein modifizierter P-Star-Ansatz, Februar 1999.

Nr. 61 Flaig, G. und H. Rottmann, Direkte und indirekte Beschäftigungseffekte von Innovationen. Eine empirische Paneldatenanalyse für Unternehmen des westdeutschen Verarbeitenden Gewerbes, Februar 1999.

Nr. 62 Sinn, H.-W. und M. Thum, Gesetzliche Rentenversicherung: Prognosen im Vergleich, Juni 1999.

Nr. 63 Goldrian, G. und B. Lehne, ASA-II im empirischen Vergleich mit anderen Saisonbereinigungsverfahren, Oktober 1999.

Nr. 64 Thum, M. und J. von Weizsäcker, Implizite Einkommensteuer als Meßlatte für die aktuellen Rentenreformvorschläge, Dezember 1999.

Nr. 65 Gerstenberger, W., Sectoral Structures and Labour Productivity by Region, December 1999.

Nr. 66 Sinn, H.-W., EU Enlargement and the Future of the Welfare State, March 2000.

Nr. 67 Möschel, W., Megafusionen ohne Ende - besteht ordnungspolitischer Handlungsbedarf?, Juli 2000.

Nr. 68 Nam, Ch.W., R. Parsche, and M. Steinherr, The Principles of Parallel Development of Fiscal Capacity between State and Municipalities as Useful Benchmarks for the Determination of the Intergovernmental Grants in Germany, August 2000.

Nr. 69 Nam, Ch.W., R. Parsche und B. Reichl, Mehrwertsteuer-Clearing in der EU auf Basis der Volkswirtschaftlichen Gesamtrechnungen - Modellrechnung anhand der Länder Frankreich, Italien und Vereinigtes Königreich, August 2000.

Nr. 70 Adler, U., Costs and Benefits in Occupational Health and Safety, September 2000.

Nr. 71 Langmantel, E., The Impact of Foreign Trade on the German Business Cycle. An Empirical Investigation, January 2001.

Nr. 72 Nam, Ch.W., R. Parsche, and B. Reichl, Municipal Finance and Governance in Poland, the Slovak Republic, the Czech Republic and Hungary, January 2001.

Nr. 73 Nam, Ch.W., R. Parsche, and B. Schaden, Measurement of Value Added Tax Evasion in Selected EU Countries on the Basic of National Accounts Data, February 2001.

Nr. 74 Raabe, K., Assessment of the Leading Indicator Properties of Economic Variables for France, Germany, and Italy, April 2002.

Nr. 75 Radulescu, D.M., Assessment of Fiscal Sustainability in Romania, May 2002.

Nr. 76 Raabe, K., Out-of-Sample Forecast Performance of Economic Variables for France, Germany, and Italy, August 2002.

Nr. 77 Gebauer, A., Ch.W. Nam, and R. Parsche, Lessons of the 1999 Abolition of Intra-EU Duty Free Sales for Eastern European Candidates, December 2002.

Nr. 78 Nam, Ch.W. and D.M. Radulescu, The Role of Tax Depreciation for Investment Decisions: A Comparison of European Transition Countries, December 2002.

Nr. 79 Osterkamp, R., German Public Health Insurance: Higher Co-payments and Everybody Is Better off - the Case for Differentiated Co-payment Rates, January 2003.

Nr. 80 Kunkel, A., Zur Prognosefähigkeit des ifo Geschäftsklimas und seiner Komponenten sowie die Überprüfung der „Dreimal-Regel", März 2003.

Nr. 81 Fehn, R., Strukturwandel und europäische Wirtschaftsverfassung: Gibt es einen Zielkonflikt zwischen Effizienz und Sicherheit?, April 2003.

Nr. 82 Gebauer, A, Ch.W. Nam and R. Parsche, Is the Completion of EU Single Market Hindered by VAT Evasion?, June 2003.

Nr. 83 Meurers, M. Incomplete pass-through in import markets and permanent versus transitory exchange-rate shocks, December 2003.

Nr. 84 Gebauer, A., Ch.W. Nam and R. Parsche, Regional Technology Policy and Factors Shaping Local Innovation Networks in Small German Cities, January 2004.

Nr. 85 Nam, Ch.W. and D.M.. Radulescu, Does Debt Maturity Matter for Investment Decisions?, February 2004.

Nr. 86 Beck, D., Algorithmus zur Zerlegung von gewissen Fragebögen in Komponenten, Februar 2004.

Nr. 87 Pohl, C., Makroökonomische Auswirkungen der EU-Osterweiterung, Februar 2004.


[^0]:    * I wish to thank the seminar participants at the ESPE Conference 2003 in New York, at the EALE Conference 2003 in Sevilla and in particular Adrian Masters, Klaus Schmidt and Simone Kohnz for their useful comments. The usual disclaimer applies.

[^1]:    ${ }^{1}$ The details of the derivation can be found in M ortensen and Neuman (1988).

[^2]:    ${ }^{2} \mathrm{~A}$ production function where inputs are independent is the same as assuming two different firms are operating in diПerent labor markets. Furthermore, since all wages on the support of both occupation-specific wages o oler distributions must promise the same profit in equilibrium, it follows that any combination of wages is an equilibrium.

[^3]:    ${ }^{3}$ The closed form solution to the wage o $\square$ er distributions satisfies the FOC and SOC, as shown in the appendix.

